LinAlg Quiz: Pseudoinverse and Determinant

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December 2023

1 Quiz

Let $A, B \in \mathbb{R}^{n \times n}$ and $W \in \mathbb{R}^{m \times n}$:

- 1. How is det(A) related to det(7A)?
- 2. The determinant is only defined for square matrices
- 3. If two rows or columns of A are identical, det(A) = 0
- 4. Applying elimination matrices on A doesn't change det(A)
- 5. $\det(A) = -\det(A^T)$
- 6. det(AB) = det(B) det(A)
- 7. $det(A^2) = det(A) det(A)$

8.
$$\det(A^{-1}) = \frac{1}{\det(A)}$$

- 9. $WW^+ = I$ or $W^+W = I$
- 10. If W has full column rank, $W^T W$ has full row rank and is surjective
- 11. If W has full row rank, $m \ge n$ and W is surjective